

# 2nd Feasibility Study of a Muon Storage Ring Neutrino Factory

US Muon Collaboration

Oxford 11/2001

R. B. Palmer (BNL)

- Today 14.15 US studies of Neutrino Factory  
Study 1, Study 2
- Wed. 12.00 Other studies,  
Experimental Programs, inc. MICE
- Thur. 12.00 Other Ideas:  
CERN & KEK Schemes  
longitudinal cooling, bunched phase rotation,  
FFAG's, Colliders, Radioactive beam neutrinos
- Fri. 16.15 The big picture:  
hadron, electron, muon colliders, neutrino factories

# Feasibility Study 1

- Commissioned by FNAL Director
  - FNAL Site specific (where relevant)
  - FNAL + Collaboration
  - Ed. Finley, Holtkamp (April 2000)
- 
- Emphasize Feasibility
  - allow "Entry Level" Performance

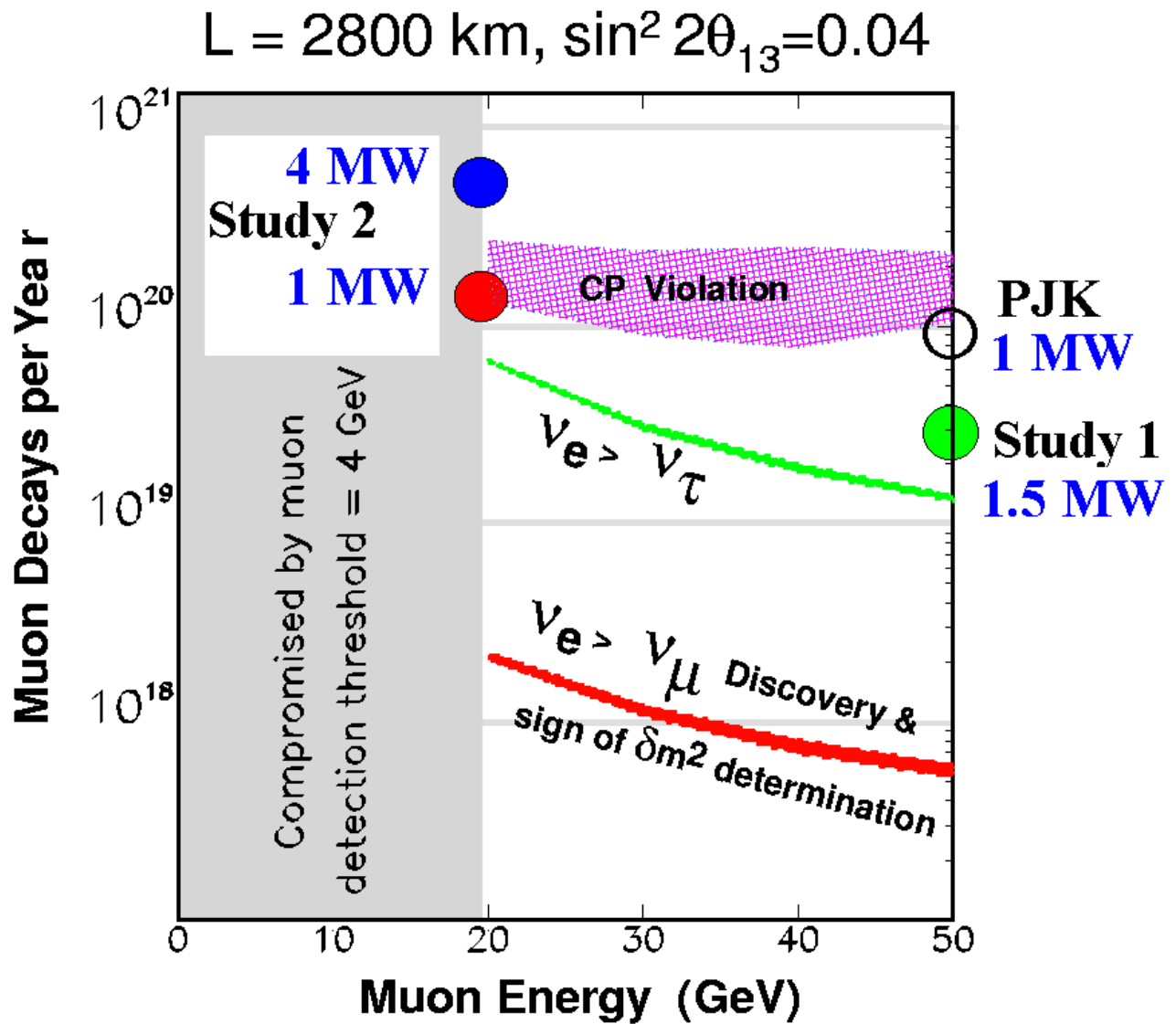
Feasible, but less performance

## Feasibility Study 2

- Commissioned by BNL Director
  - BNL Site specific (where relevant)
  - BNL + Collaboration
  - Edd. Ozaki, Palmer, Zisman
  - Closeout May 4 2001
- 
- Build on Study 1
  - Maintain Feasibility
  - Raise Performance

Feasible, and  $6 \times \mu/p$

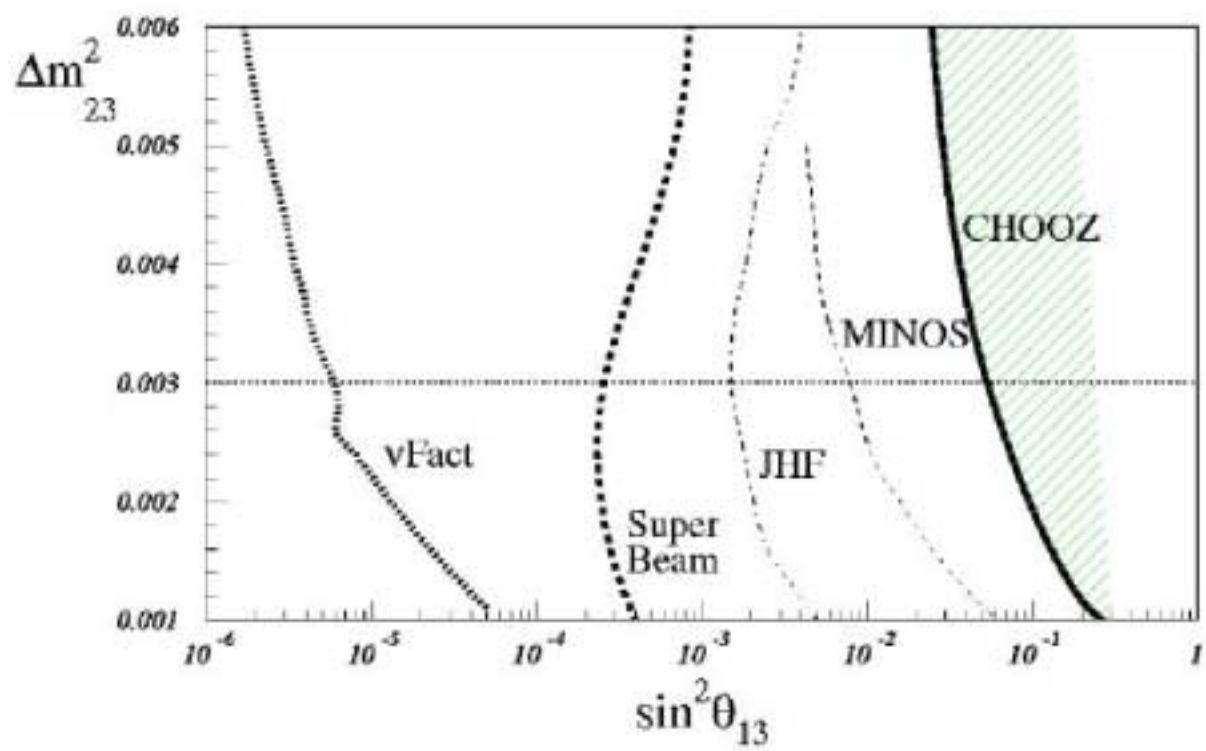
# Physics Reach



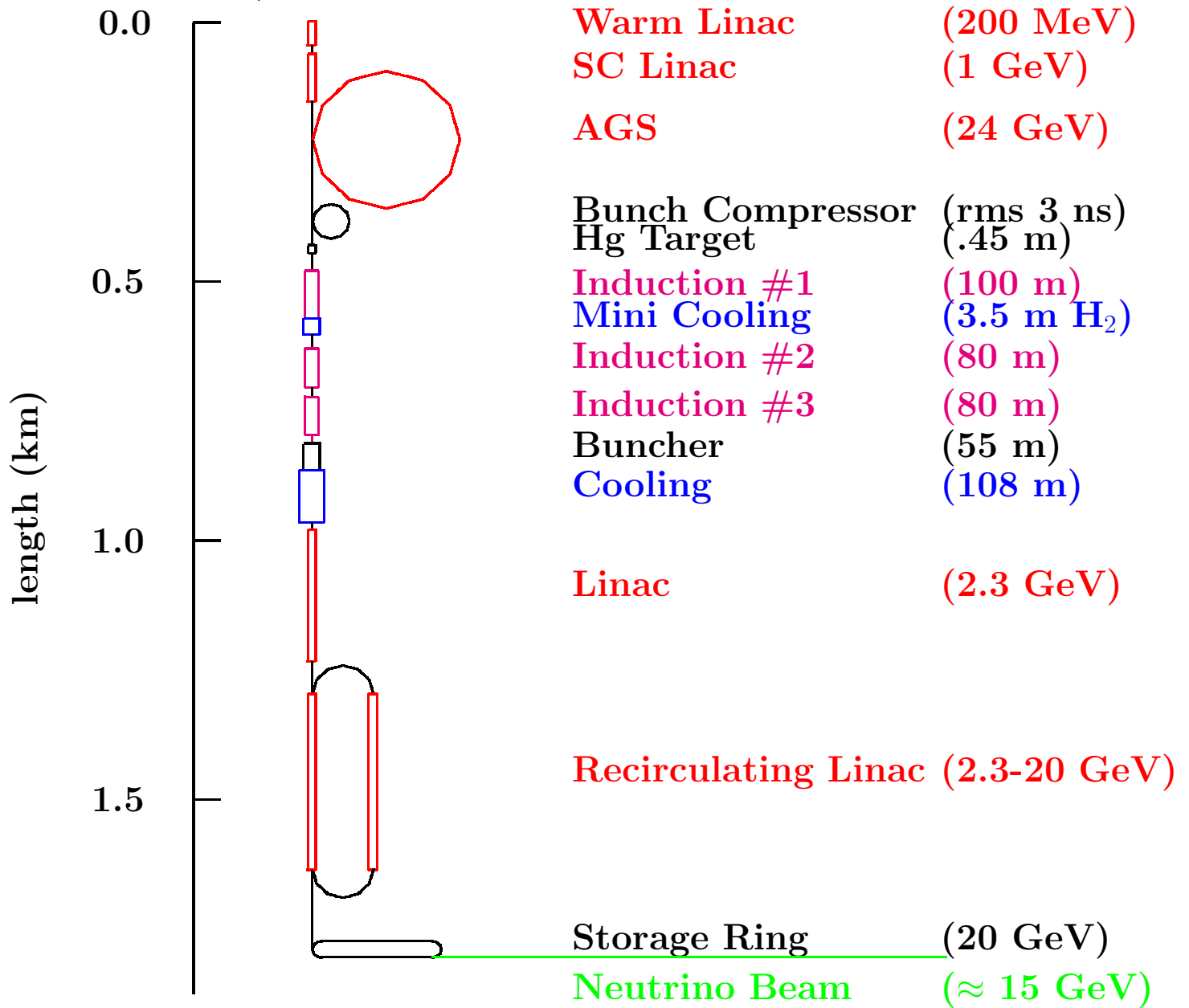
- muon decays in straight section /  $1 \cdot 10^7 \text{ sec}$
- For Detector mass 50 kT
- Best distance: 2000 - 3000 km

WIPP=2900 km    Homestake=2500 km

# Comparisons

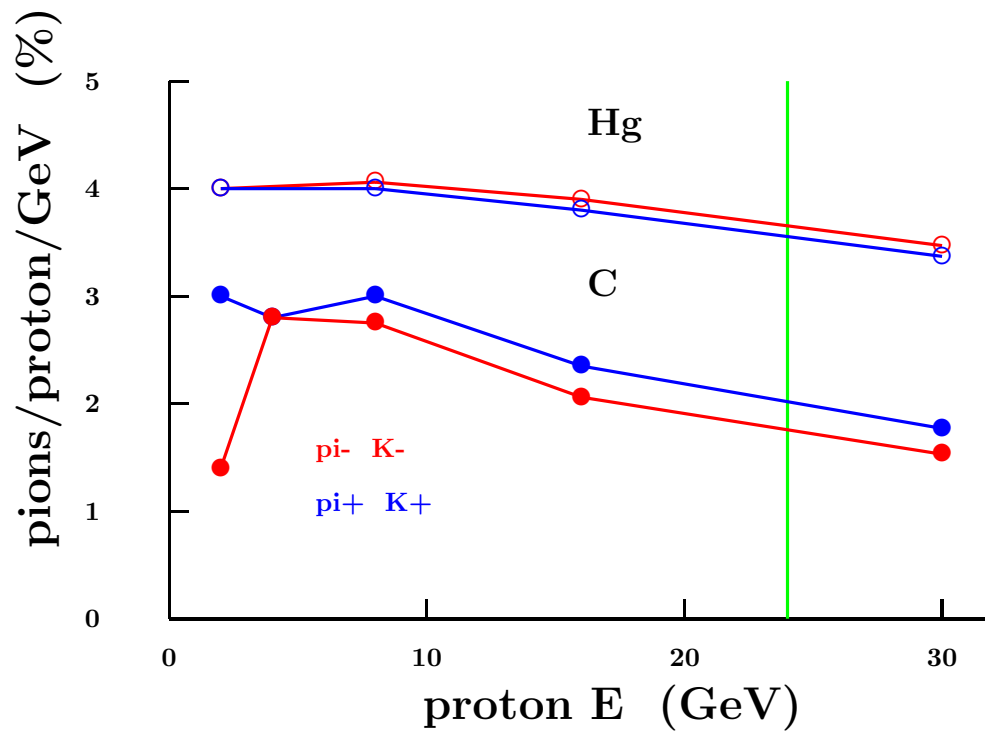


# Schematic



# PION PRODUCTION

For 50 - 800 GeV/c, pions/proton  
divided by proton energy in GeV:



- $\text{Hg} \approx 2 \times \text{C}$
- Low energy slightly better than high
- But harder to get short p bunch

# PROTON DRIVER

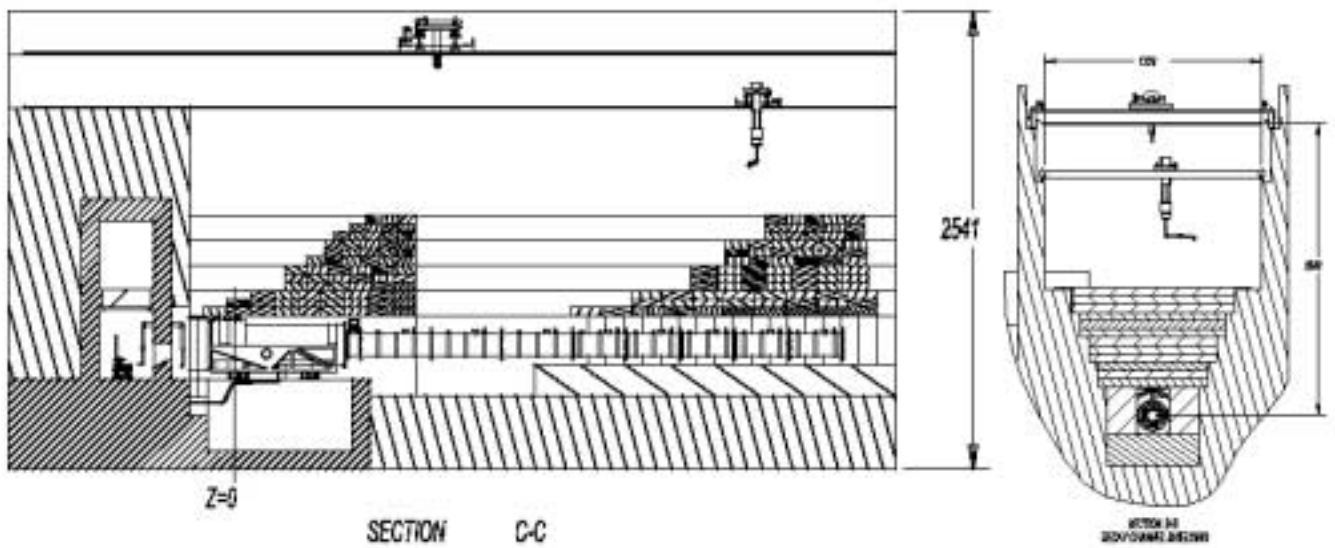
- 1 MW BNL AGS Upgrade
  - New (SNS like) SC Linac
  - Upgraded AGS ( $.5 \rightarrow 2.5$  Hz)
  - 6 single bunch extractions



- 4 MW further upgrade
  - Increases linac  $E \rightarrow 2 \times$  charge
  - Accumulator Ring  $\rightarrow 5$  Hz
  - Bunch Compressor
- Similar performance with new 16 GeV Booster at FNAL



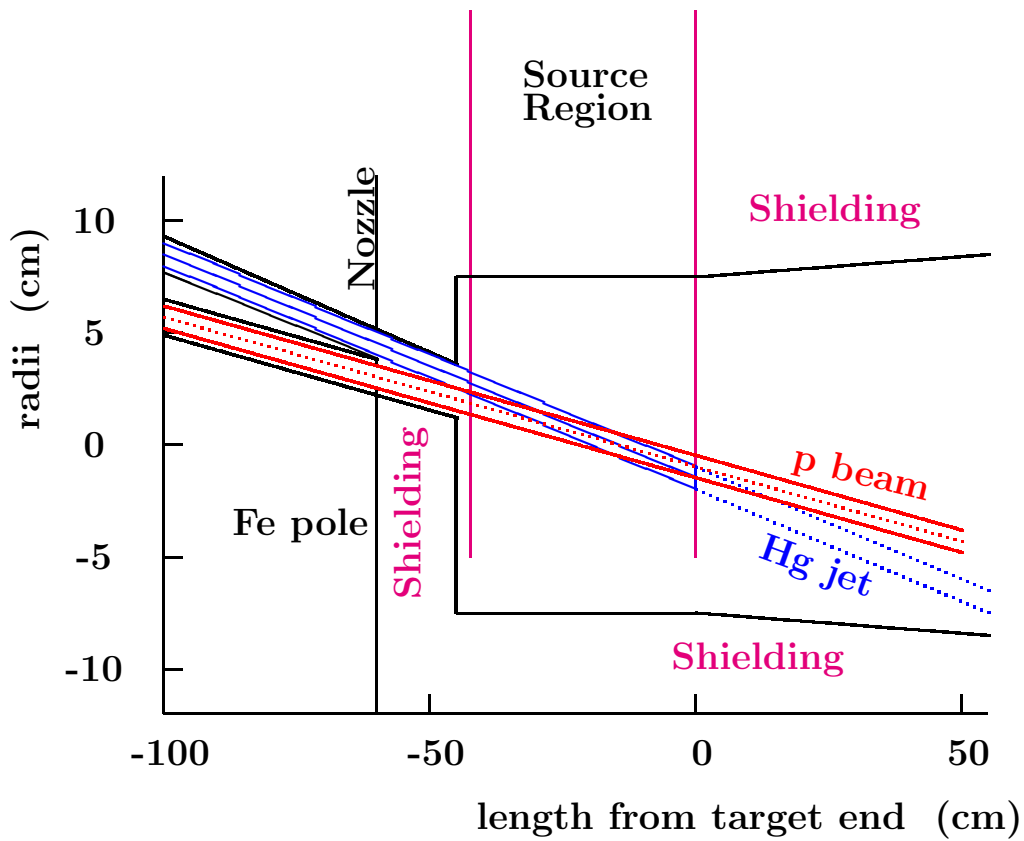
# Target Area for 4 MW



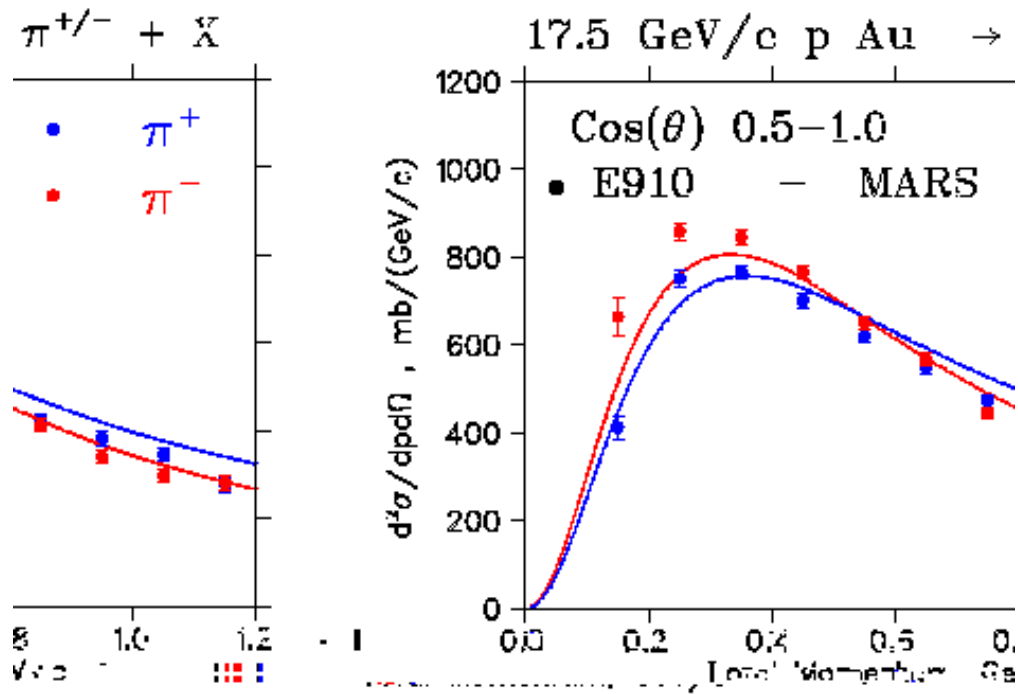
# TARGET

## Mercury jet Target

- $\approx 2 \times$  Carbon (of study 1)
- 20 m/s replaces disturbed
- Nozzle inside field
- OK to 4 MW ?



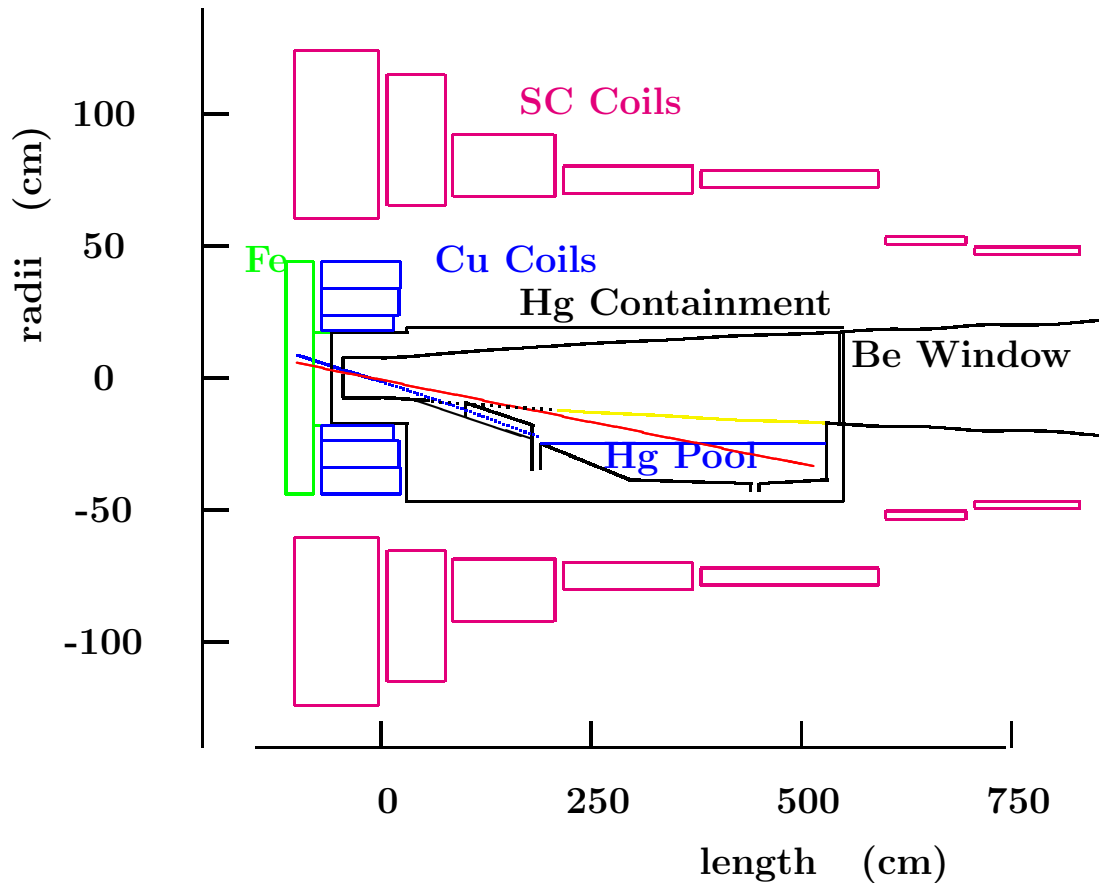
## Where are the pions ?



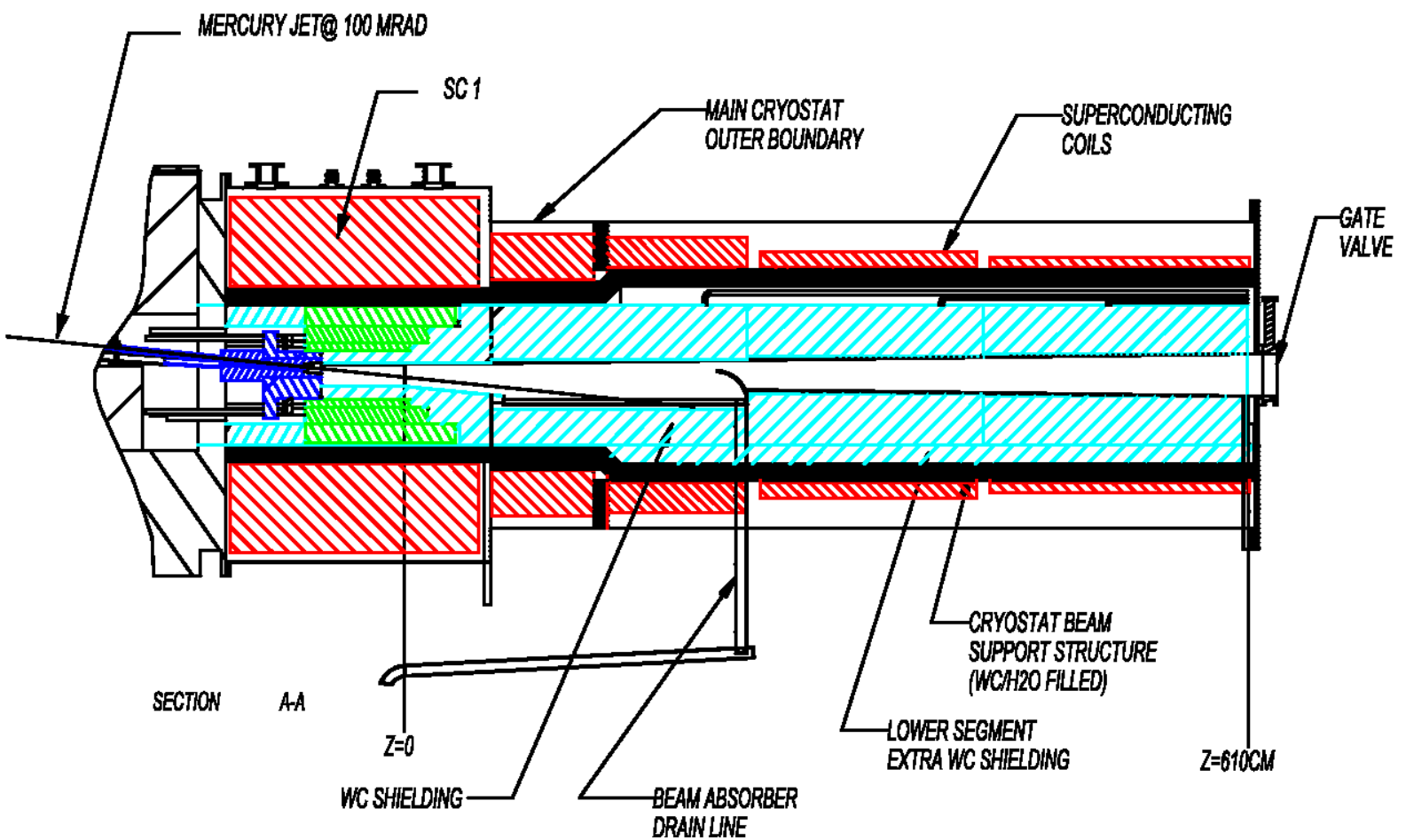
- Peak at low momenta  $\approx 300$  MeV/c
- $p_{\perp} \approx 200$  MeV/c
- Angles large  $\approx 45$  deg.
- Use 20 T, 8 cm rad, Solenoid
- Captures all below 240 MeV/c
- Slow taper field to 1.25 T
- Pions are folded forward

# Capture Solenoid & Dump

- 20 T hybrid magnet
  - Hollow Conductor Insert
  - Superconducting Outsert
- Taper field to 1.25 T in 18 m
- Mercury pool Beam Dump



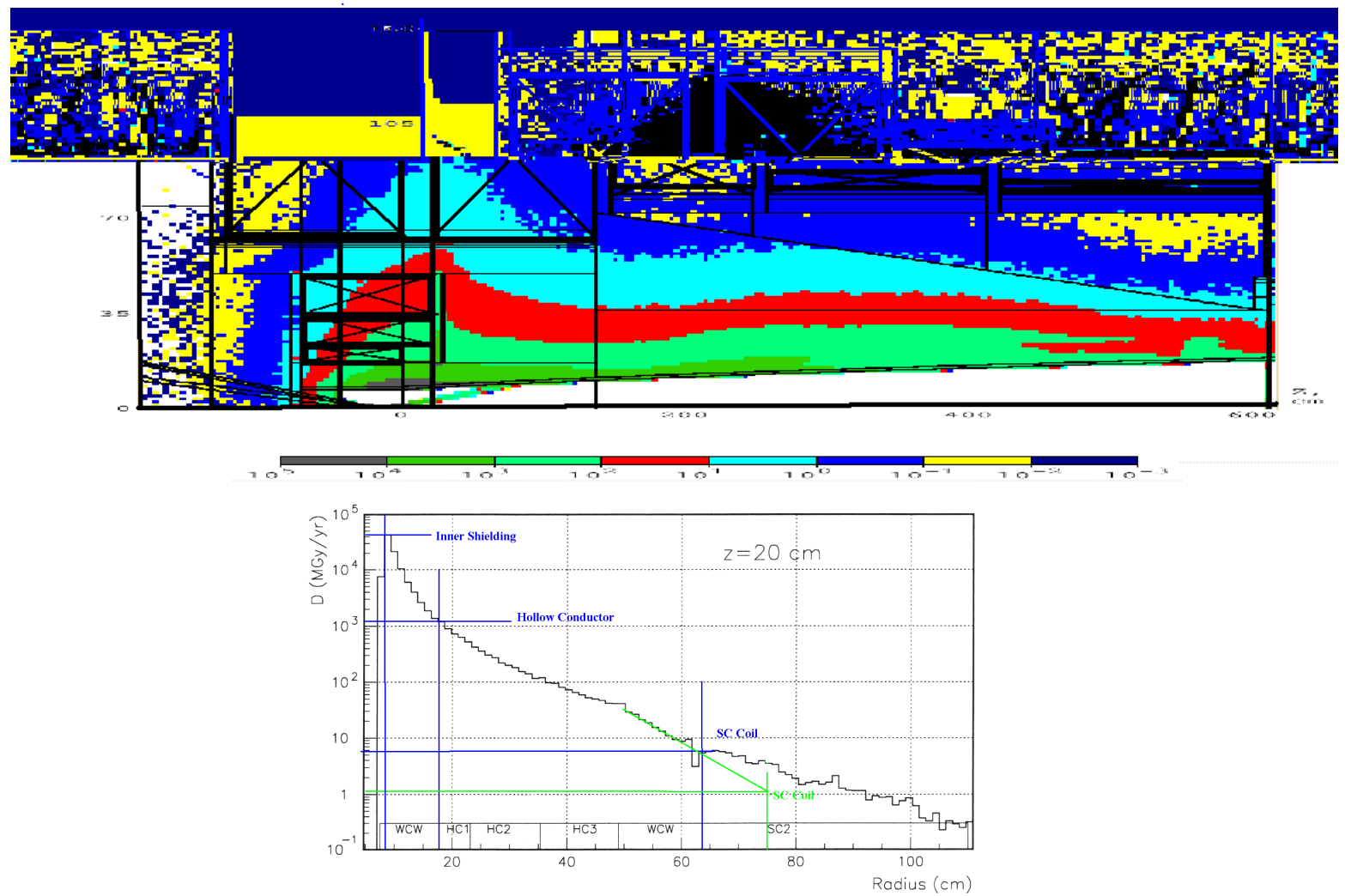
# Layout



# Study 2 Radiation Levels

from Mokhov

for radiation 1 year  $\equiv 2 \cdot 10^7$  s



Component	radius cm	1 MW Dose/yr Grays	Max Dose Grays	1MW Life years	4 MW life years
Inner Shielding	7.5	$5 \cdot 10^{10}$	$10^{12}$	20	5
Hg Containment	18	$10^9$	$10^{11}$	100	25
Hollow Conductor	18	$10^9$	$10^{11}$	100	25
Superconductor	65 (75)	$5 (1.2) \cdot 10^6$	$10^8$	20 (80)	5 (20)

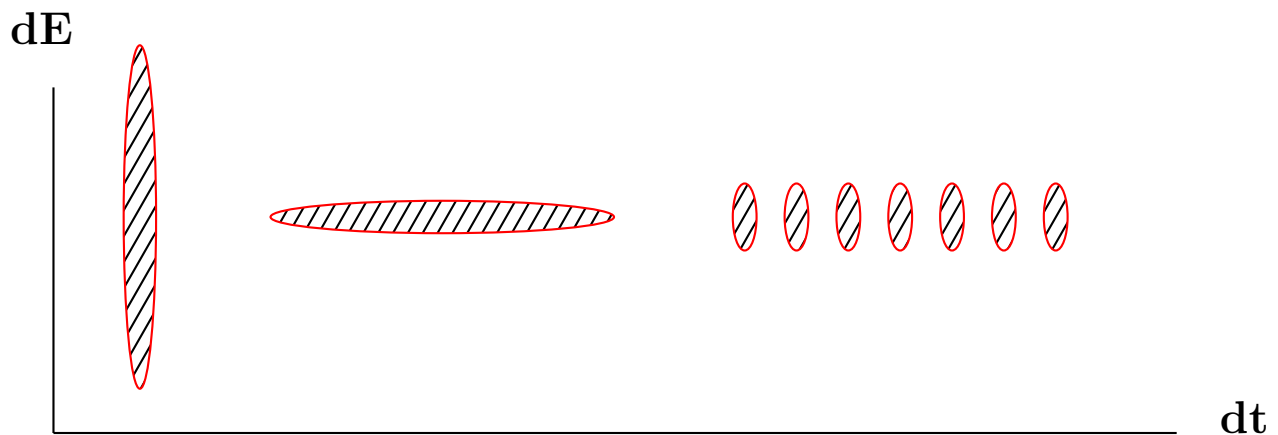
## PROBLEM

- Initial pions have rms  $dp/p \approx 100\%$
- rms Acceptance of cooling  $\approx 8\%$

## SOLUTION:

### Phase Rotate & Re-Bunch

- Increase  $dt$
- Decrease  $dE$



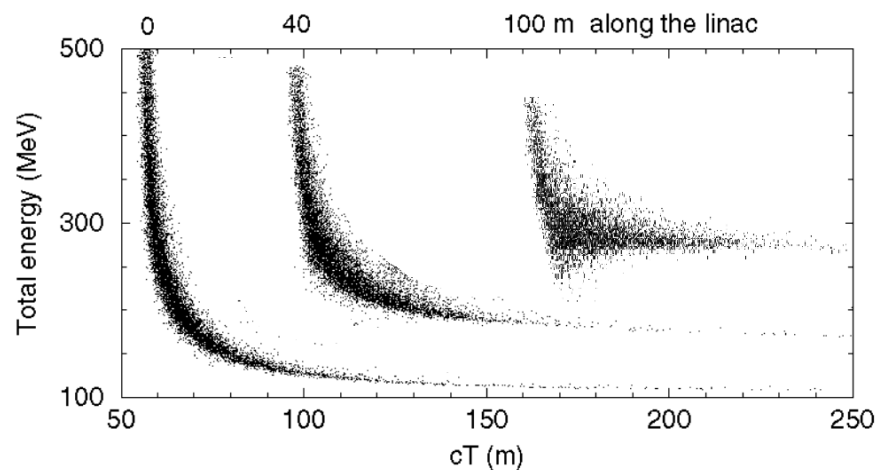
# Simple Phase Rotation

## 1. Drift

## 2. Induction Linac to reduce $dE/E$

- Energy spread non uniform
- $dp/p$  rms  $\approx 6\%$

e.g. Study 1



**Figure 6:** Beam distributions in E-cT phase space along the induction linac. Distributions from  $L = 0$ , 20, 60, and 100 m are shown.

## 3. Bunch

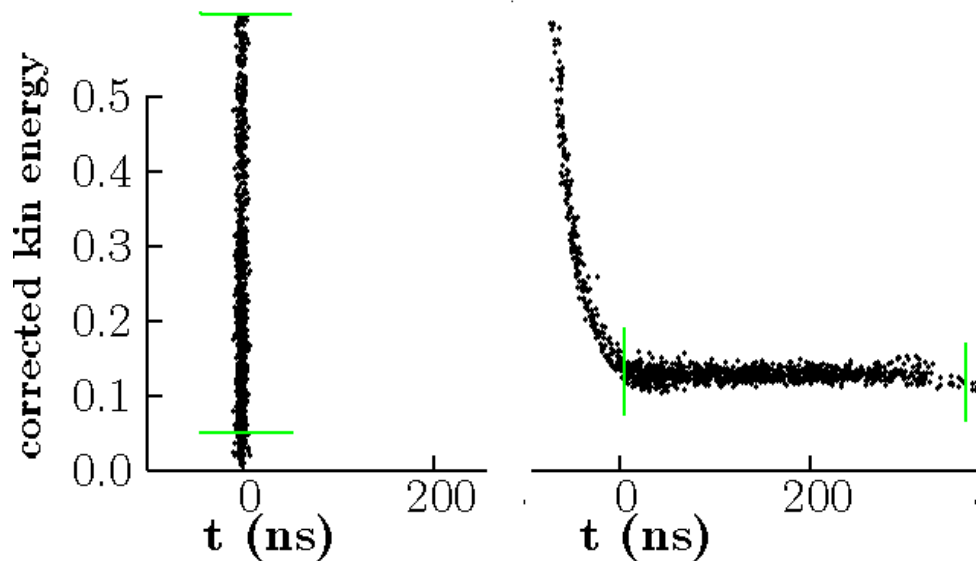
- $dp/p$  rms  $\approx 18\%$  **too large**



# Non-distorting

1. 30 m Drift
2. Induction Linac to modify  $E$  vs  $t$
3. Second drift ( $\approx 100$  m)
4. 2nd Induction Linac to reduce  $dE/E$ 
  - Energy spread more uniform
  - $dp/p$  rms  $\approx 3\%$

## Study 2

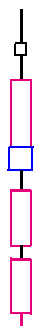


## 5. Bunch

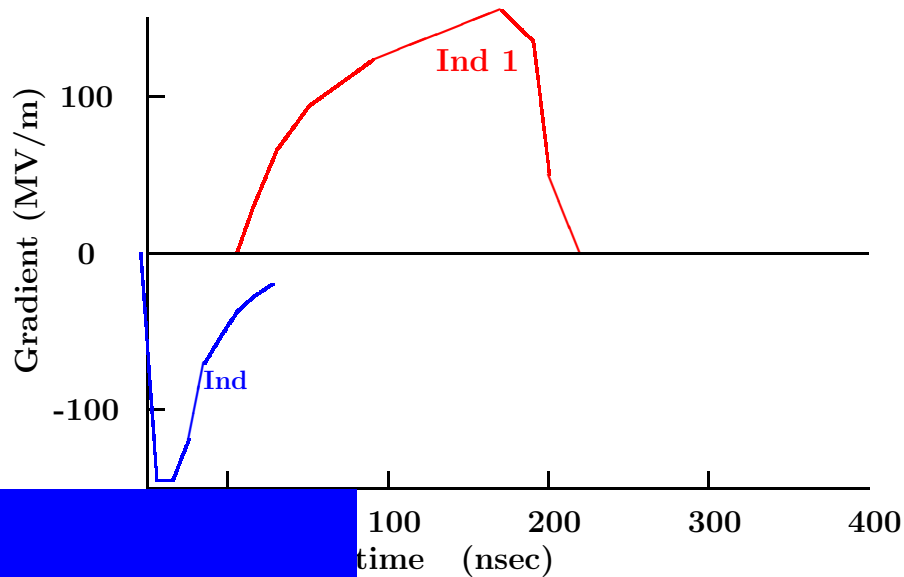
- $dp/p$  rms  $\approx 8\%$  **OK**

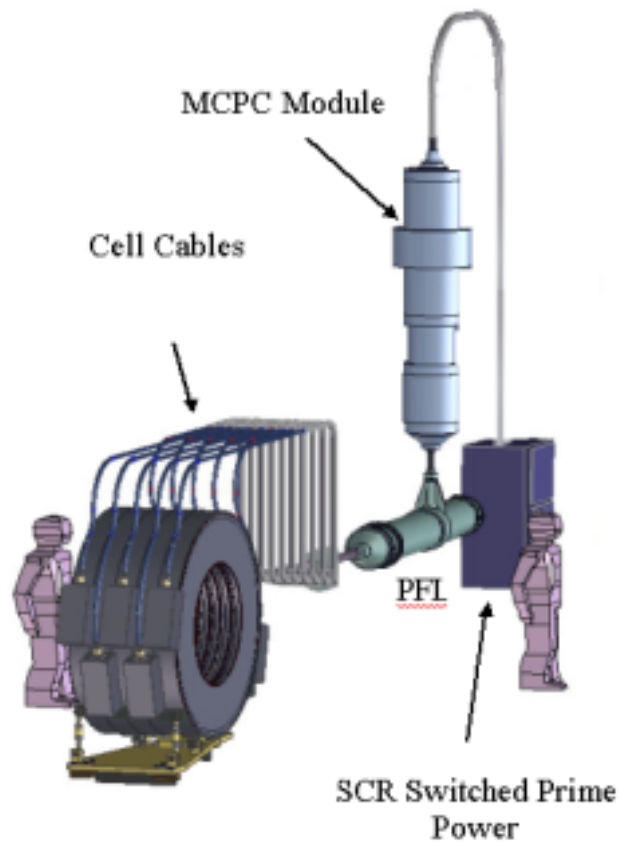
## Study 2 Rotation

- Non-distorting
- 3 Unipolar Units
- Single pulses (FS1: 4)
- total length 260 m (FS1: 100)

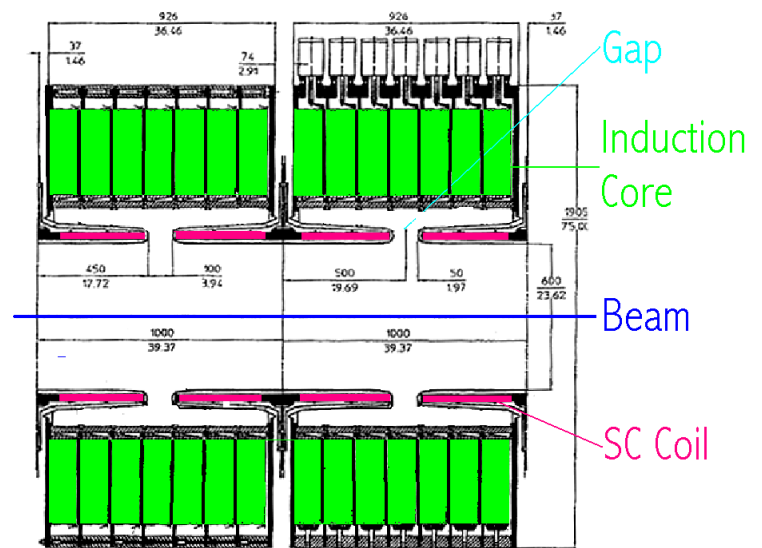


Hg Target	(.45 m)
Induction #1	(100 m)
Mini Cooling	(3.5 m H <sub>2</sub> )
Induction #2	(80 m)
Induction #3	(80 m)



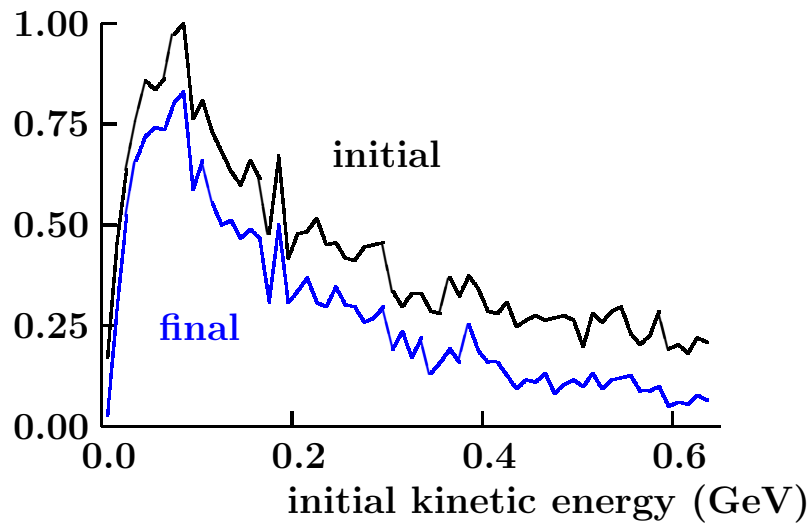


**2m Section**  
 95 cm radius  
 similar to  
 ATA or DARHT  
 but  
 Superconducting  
 inside coil



# Performance

From target to phase rotation:

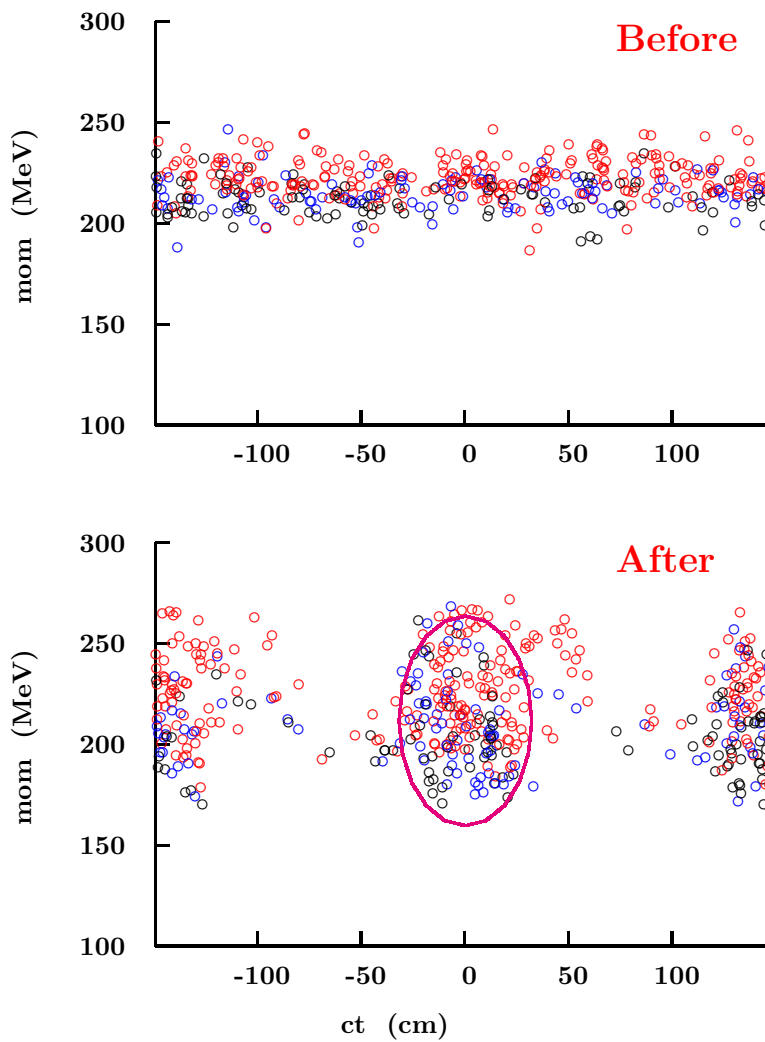


# RF BUNCHER

Three stages:

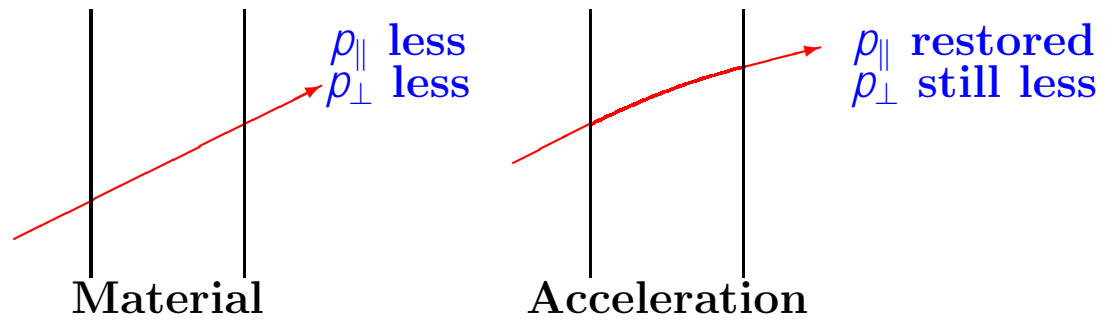
- 1: Low field 200 MHz rf + 400 MHz harmonic
2. Med. field 200 MHz rf + 400 MHz harmonic
3. Higher field 200 MHz rf

Similar to Study 1

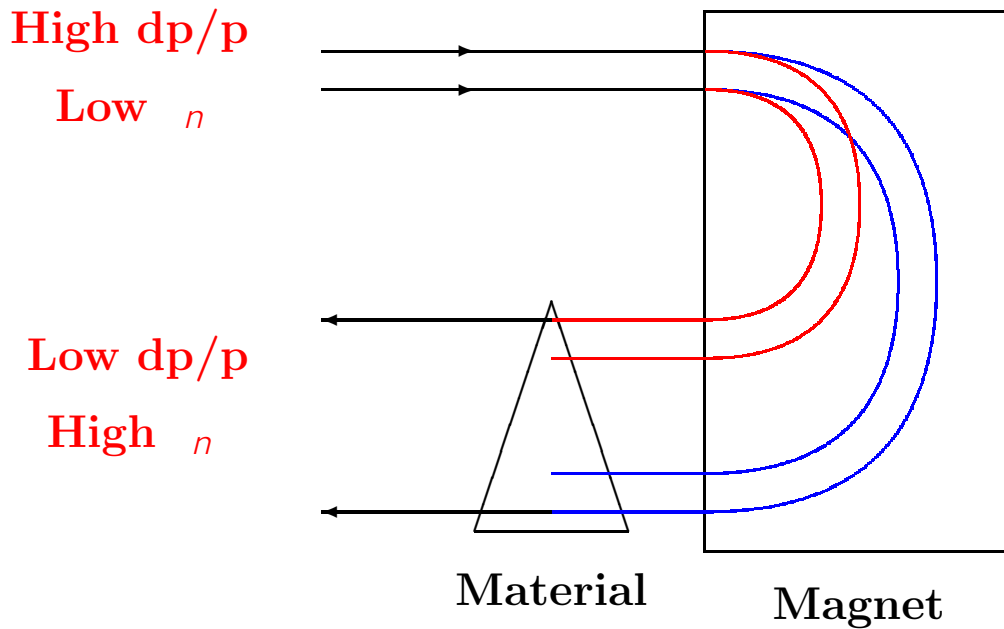


# COOLING CONCEPTS

## • TRANSVERSE



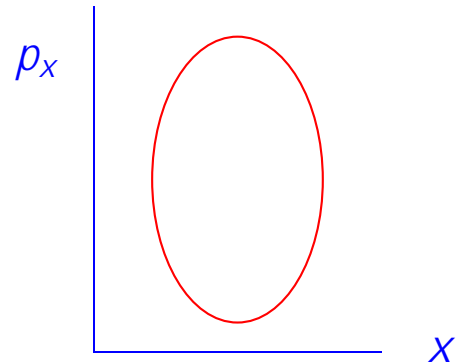
## • LONGITUDINAL EMIT EXCH



# WHAT IS EMITTANCE

$$\text{normalized emittance} = \frac{\text{PhaseSpaceArea}}{m c}$$

If  $x$  and  $p_x$  both Gaussian and uncorrelated, then area is an upright ellipse



$$\epsilon_{\perp} = \frac{dp_{\perp} dx}{mc} = \epsilon_x (\epsilon_v) \quad (\text{m rad})$$

$$\epsilon_{\parallel} = \frac{dp_{\parallel} dz}{mc} = dp/p_z (\epsilon_v) \quad (\text{m rad})$$

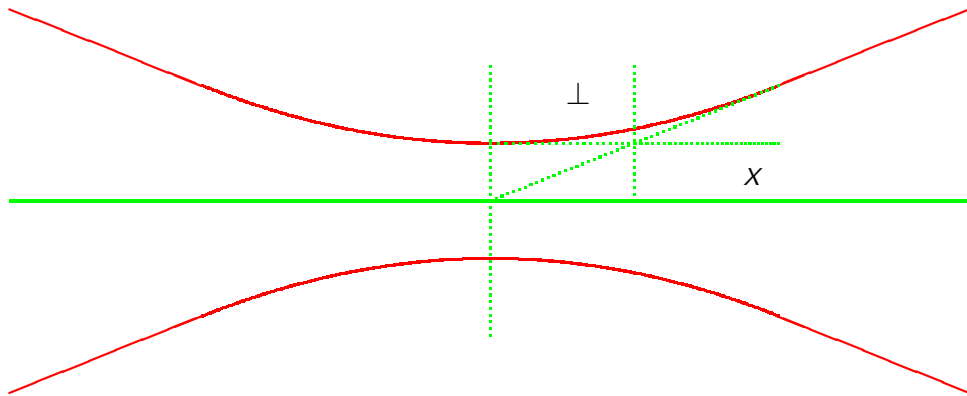
$$\epsilon_6 = \epsilon_{\perp}^2 \epsilon_{\parallel} \quad (\text{m})^3$$

Note that, by convention, the is not included in the calculated values, but added to the dimension

# WHAT IS BETA *Courant–Schneider*

Again upright ellipse, e.g. at Focus:

$$\perp = \frac{x}{\beta}$$



Then, using emittance definition:

$$x = \sqrt{\frac{\perp}{\beta} \frac{1}{\nu}}$$

and:

$$= \sqrt{\frac{\perp}{\beta} \frac{1}{\nu}}$$



# Transverse Cooling

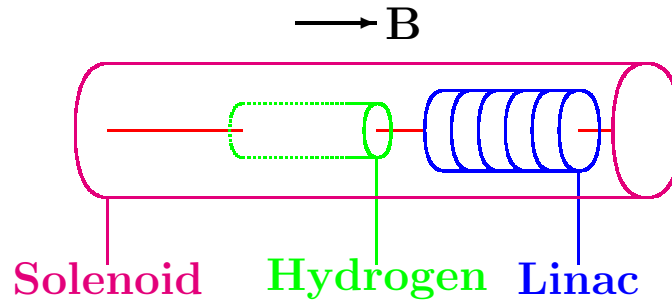
- Energy Loss lowers  $\perp$
- Coulomb Scattering Increases  $\perp$
- Equilibrium:

$$\perp \propto \perp \frac{1}{v L_R dE/dx} \propto \perp$$

- Need Low  $\perp$
- Need Low Z Material
  - Hydrogen
  - Lithium Hydride
  - Lithium

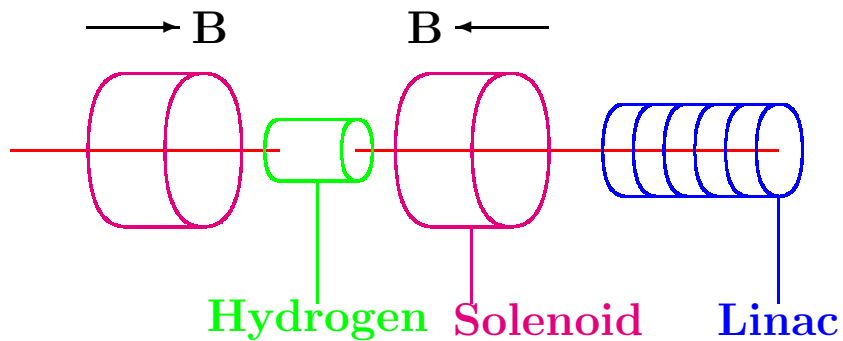
How to get low  $\perp$

## SOLENOID



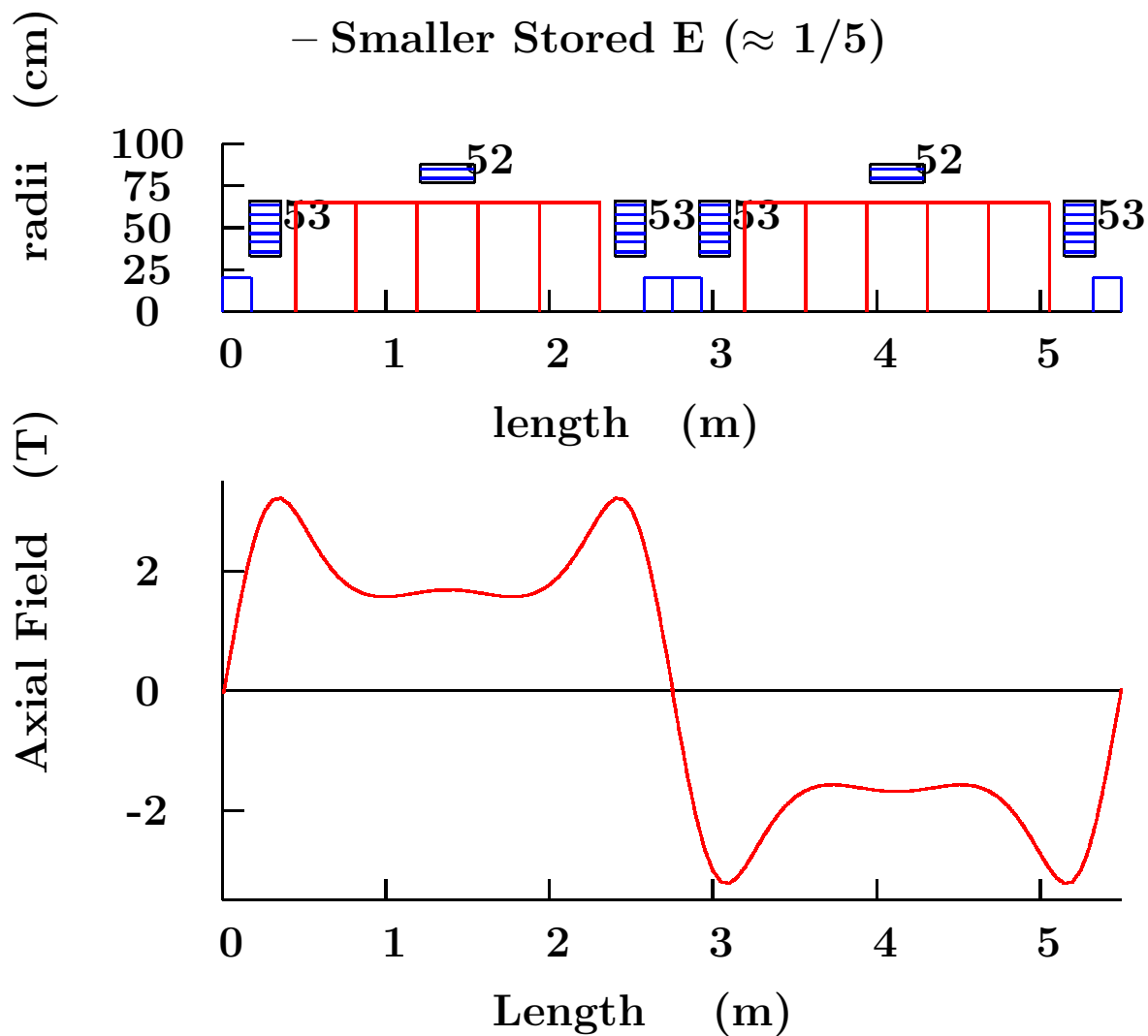
But coils are large, and direction of field must flip at least once, to avoid build up of angular momentum

## FOCUS



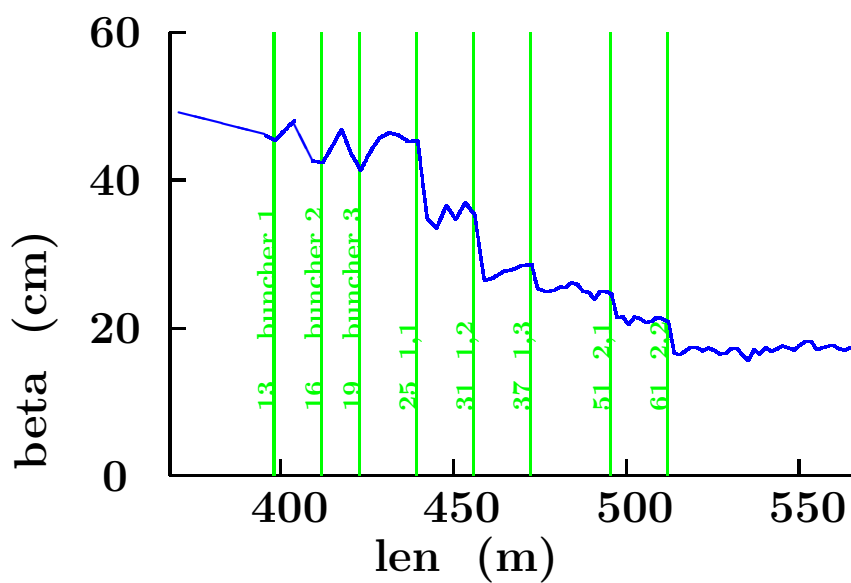
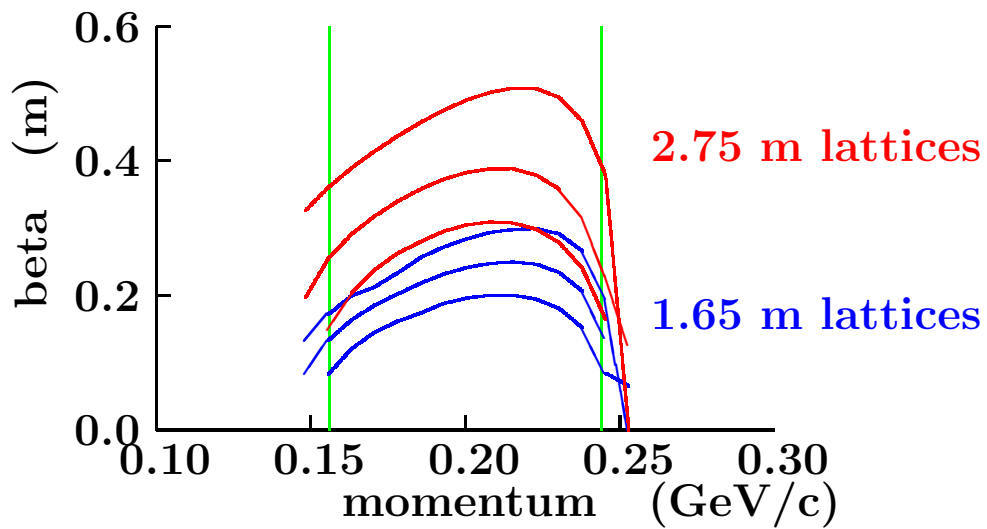
# Super FOFO Lattice

- 110 m long
- 17 MV/m RF
- Super FOFO Lattice
  - Stronger focus
  - Smaller Stored E ( $\approx 1/5$ )



## Tapered Lattices

- as emittance falls, lower betas
- maintain constant angular beam size
- maximizes cooling rate



The diagram illustrates the cross-section of the ITER tokamak, highlighting the RF cavity and LH2 module. Key components and labels include:

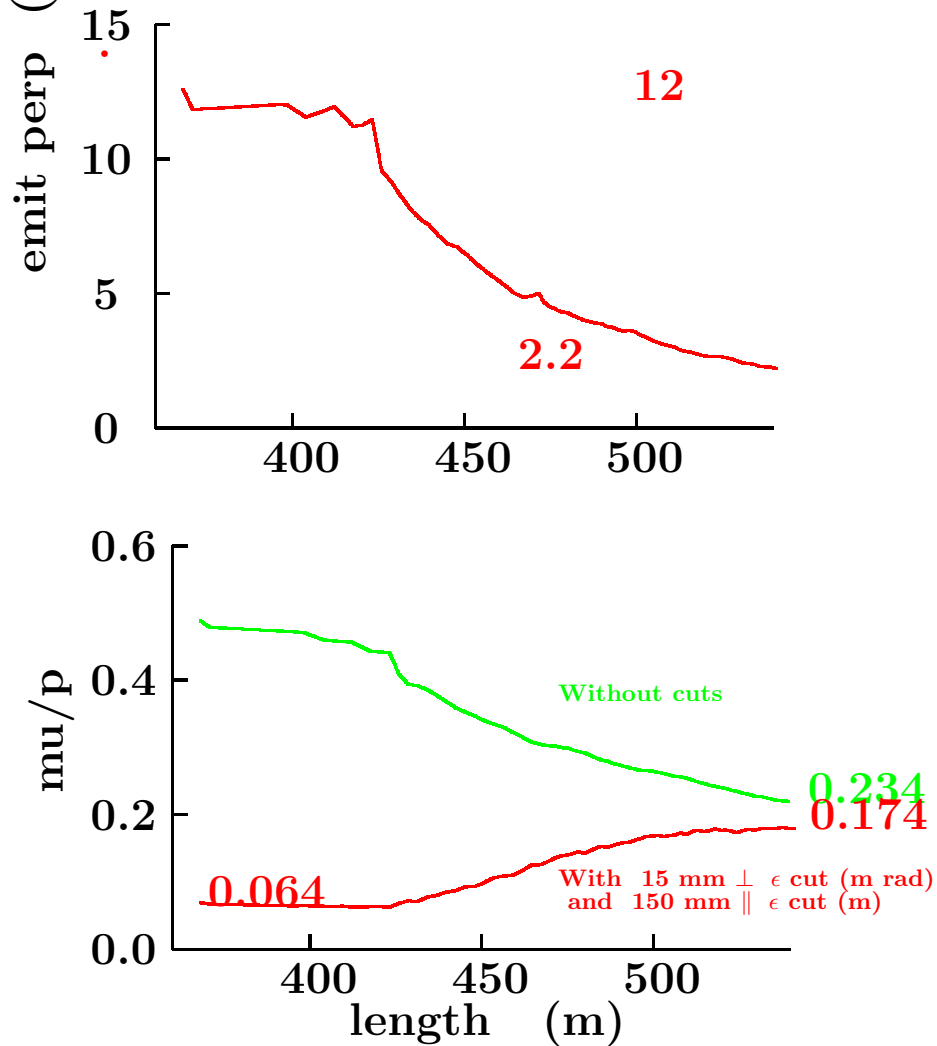
- RF CAVITY**: The central region where the RF field is applied.
- LH2 MODULE**: The liquid hydrogen module, shown in red.
- RF FEED CORNERS**: The corners where the RF feed enters the cavity.
- COLLAPSIBLE FLANGE/WEDGE**: A component at the top of the structure.
- SAFETY VENT**: A vent located at the top right.
- LH2-He HEAT EXCHANGER**: A heat exchanger for the liquid hydrogen.
- COIL SUPPORT RING**: A ring supporting the coils.
- AL WINDOW LH2**: A window for the liquid hydrogen.
- PUMP**: A pump located at the bottom right.
- COILANT SUPPLY & RETURN**: The system for supplying and returning the coilant.
- ROUGH TO LOW VACUUM**: The vacuum level in the central region.
- COIL #4** and **COIL #8**: Specific coils identified.
- ONE LATTICE LENGTH**: A dimension of  $3.75\text{m}$  ( $1233\text{ft}$ ).
- HIGH VACUUM**: The vacuum level in the central region.
- AXIAL FIELD MAXIMUM #8**: A dimension of  $6.247248\text{m}$  ( $20.51\text{ft}$ ).
- RF 301 MHz CAVITY**: The frequency of the RF field.

Technical drawing of the RFQ structure for the ESR-200 spectrometer. The diagram shows a cross-section of the structure with various components labeled and dimensions provided in both metric and imperial units.

Key components and dimensions:

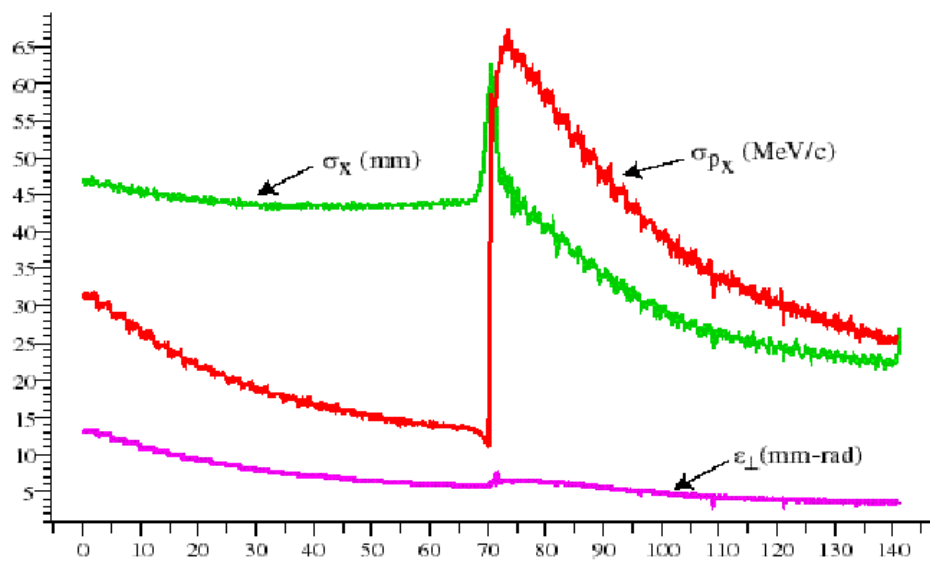
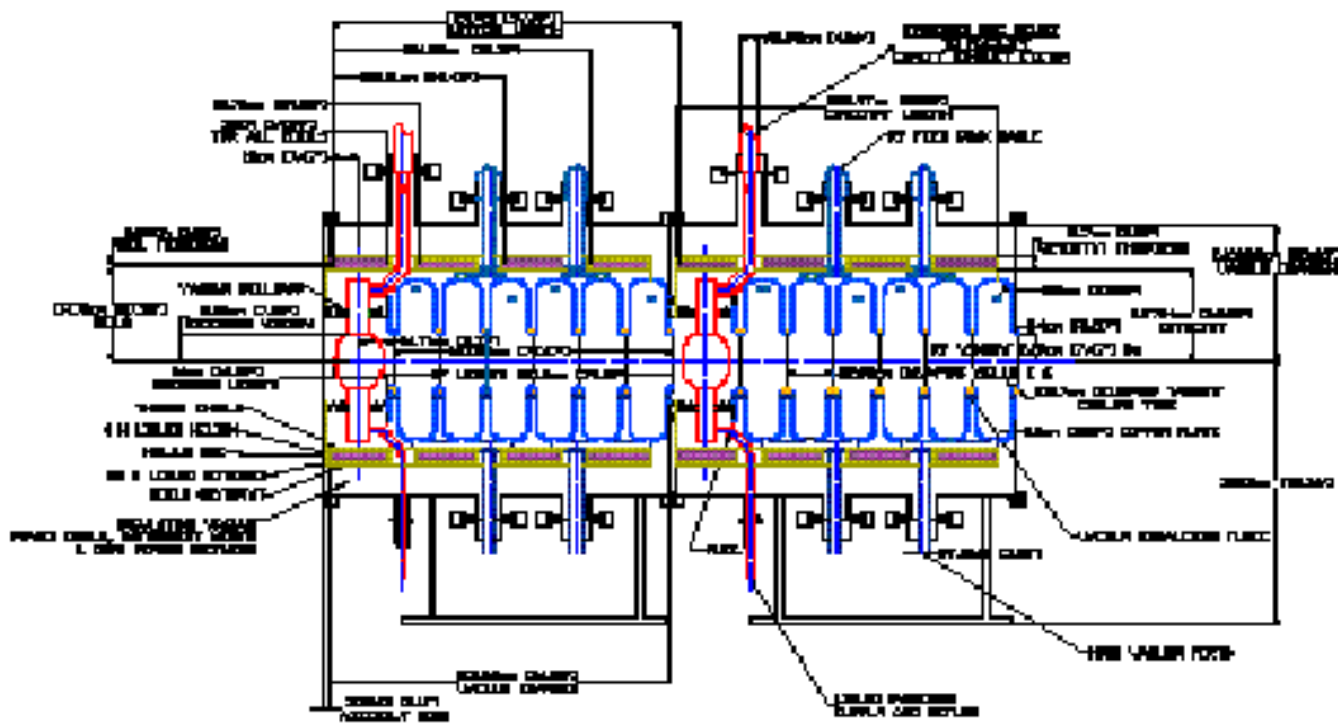
- RF FEED AT 15° ROTAT**
- SAFETY VENT**
- ACCESS BORE**:  $\phi 0.098\text{m}$  [3.84"]
- COIL SUPPORT**:  $0.06\text{m}$  [2.35"]
- ABSORBER WINDOW**:  $\text{Al WALL } t=220\mu$
- HYDROGEN WINDOW**:  $\text{rad } 0.11\text{m}$  [4.33"]
- HYDROGEN MAX**:  $\text{dl } 0.21\text{m}$  [8"]
- CRYOSTAT**:  $0.588\text{m}$  [23.15"]
- CRYOSTAT rad**:  $\phi 0.499\text{m}$  [19.64"]
- COOLANT SUPPLY AT 180°**
- HIGH VACUUM CONNECTION**:  $\text{RF } 201\text{mmH}^2\text{-CAVITY}$
- len1 of A2**:  $1.439\text{m}$  [56.65"]
- len1 of A1**:  $0.066\text{m}$  [2.60"]
- dl of A2**:  $0.145\text{m}$  [5.71"]
- dl of A1**:  $0.145\text{m}$  [5.71"]
- len1 of B**:  $0.776\text{m}$  [30.53"]
- len1 RF CENTER**:  $0.808\text{m}$  [31.81"]
- dl of B**:  $0.099\text{m}$  [3.90"]
- len1 of B**:  $0.017\text{m}$  [0.67"]
- len1 of B**:  $0.175\text{m}$  [6.89"]
- dr B**:  $0.396\text{m}$  [15.59"]
- rad B**:  $0.657\text{m}$  [25.86"]
- dr A1&A2**:  $0.33\text{m}$  [12.99"]
- rad**:  $0.199\text{m}$  [7.81"]
- rad of RF**:  $0.627\text{m}$  [24.69"]
- of VACUUM VESSEL**:  $0.801\text{m}$  [31.53"]
- Be WINDOWS**
- COIL "A1"**
- COIL "B"**
- COIL "A2"**
- COLLAPSABLE WEDGE/FLANGE**

## Cooling Performance



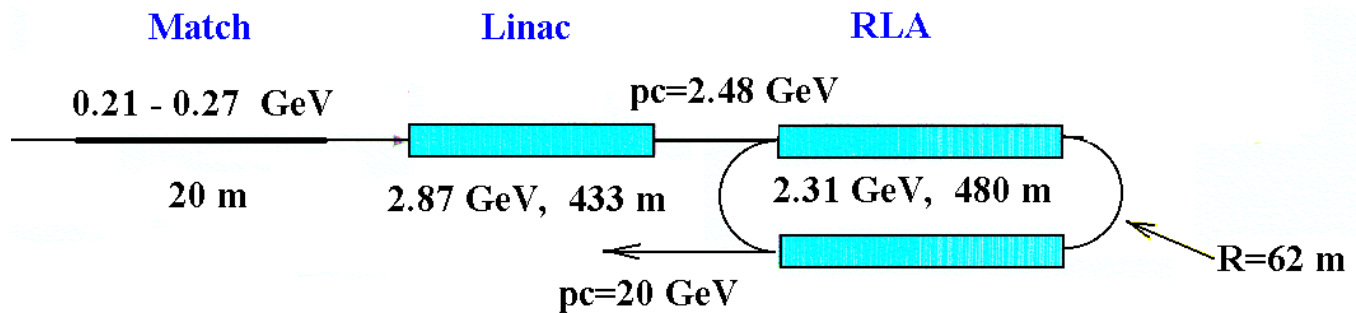
- Gain Factor = 3
- Loss from growth of long emit.
- Avoided if longitudinal cooling

## 1-2 Flip Alternative

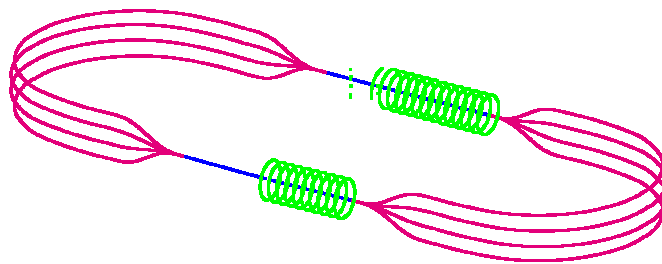


# ACCELERATION

## Linac + Recirculating Linear Accelerator (RLA)

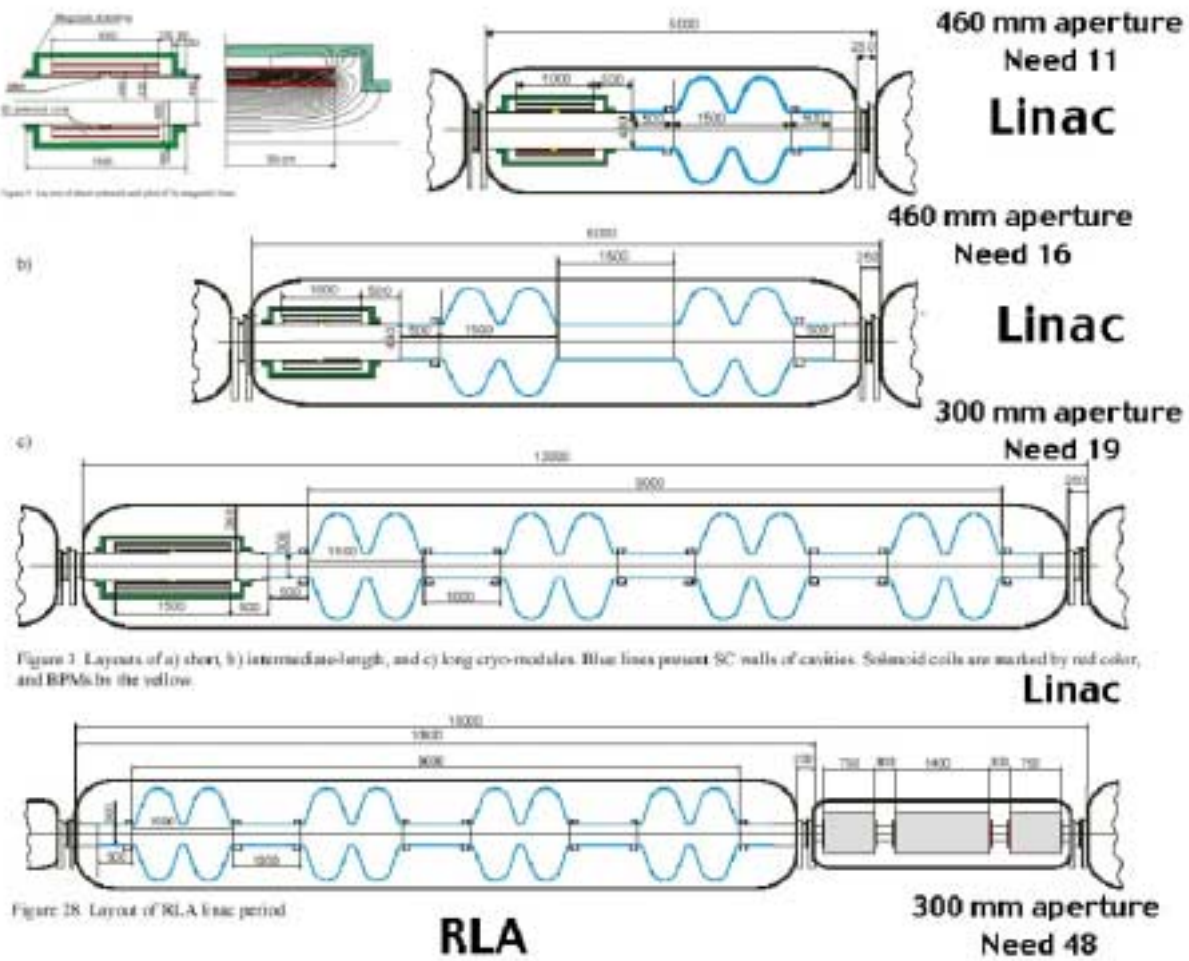


- Superconducting Linacs
- 200 MHz
- Solenoid focus in initial linac
- Quad focus in RLA



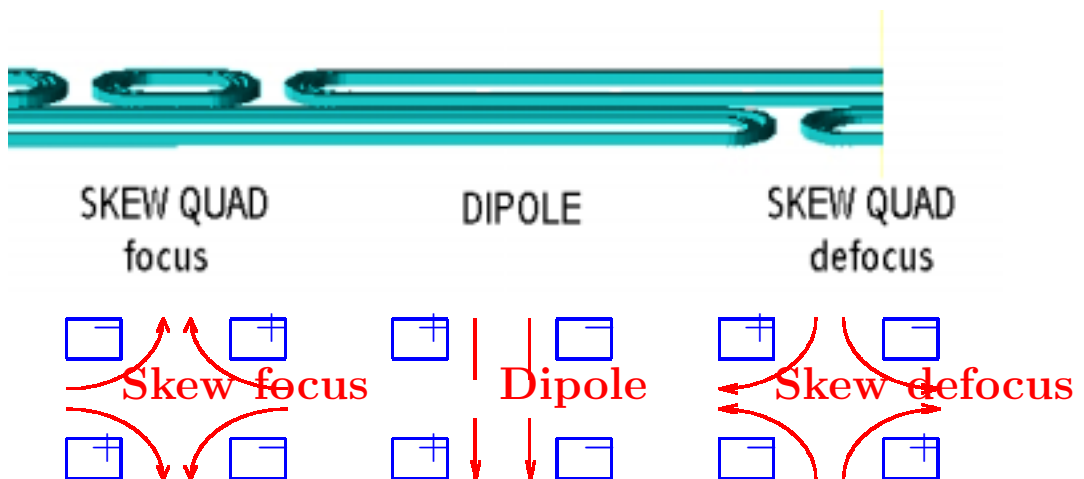
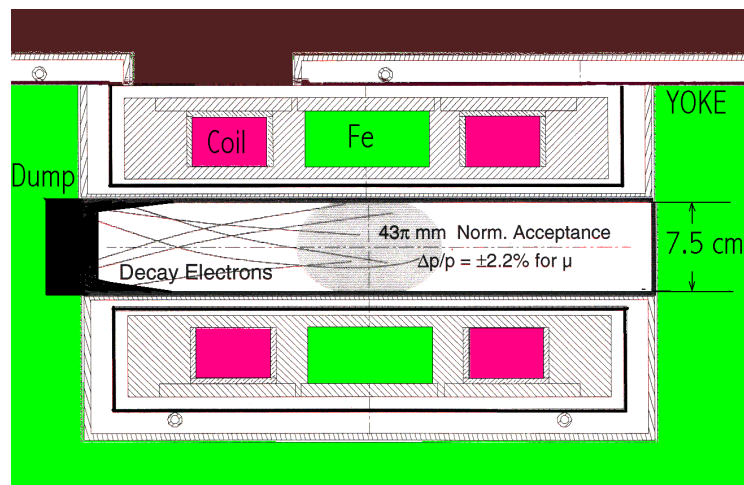


# Superconducting Cavities Cornell (200 MHz)



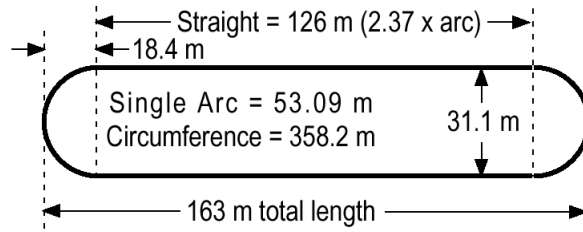
# STORAGE RING

- High Field (to maximize straight/circumference)
- 30 kW (100 W/m) Decay electrons
- Strong focus (large emittance &  $dp/p$ )
- Good longitudinal packing factor



Arc Magnet Parameters:

$B_1 = 6.93 \text{ T}$ ,  $G_1 = 0 \text{ T/m}$ ,  $L_1 = 1.89 \text{ m}$   
 $B_2 = 0 \text{ T}$ ,  $G_2 = 35.0 \text{ T/m}$ ,  $L_2 = 0.76 \text{ m}$   
Average  $B = 4.94 \text{ T}$ ,  $L_{\text{cell}} = 5.3 \text{ m}$

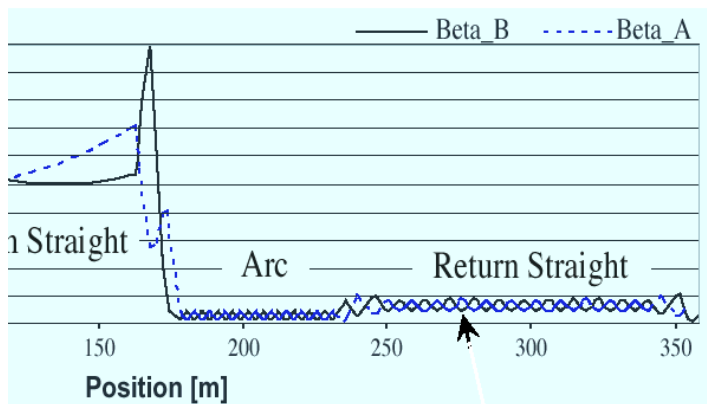


10 Cell Solution  
 $60^\circ$  Arc Cell Phase  
 $\beta_{\text{arc}} = 8.69 \text{ m}$

Empty cell has  
warm quadrupoles  
with  $G = 27.2 \text{ T/m}$ .

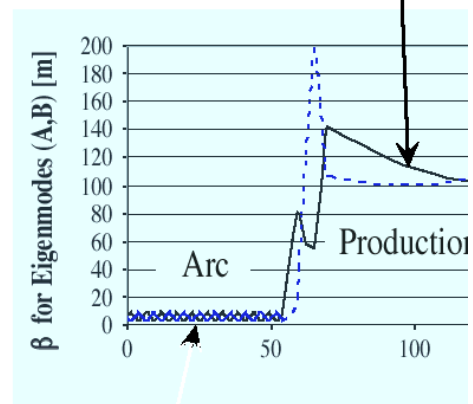
$$\text{Geometric Decay Ratio} = \frac{126 \text{ m}}{358 \text{ m}} = 0.35 \text{ per straight section}$$

section has increased  $\beta$  for reduced  
ses normal conducting quadrupoles.



53 m arc is mostly superconducting  
but has warm sections near each  
end for collimation.

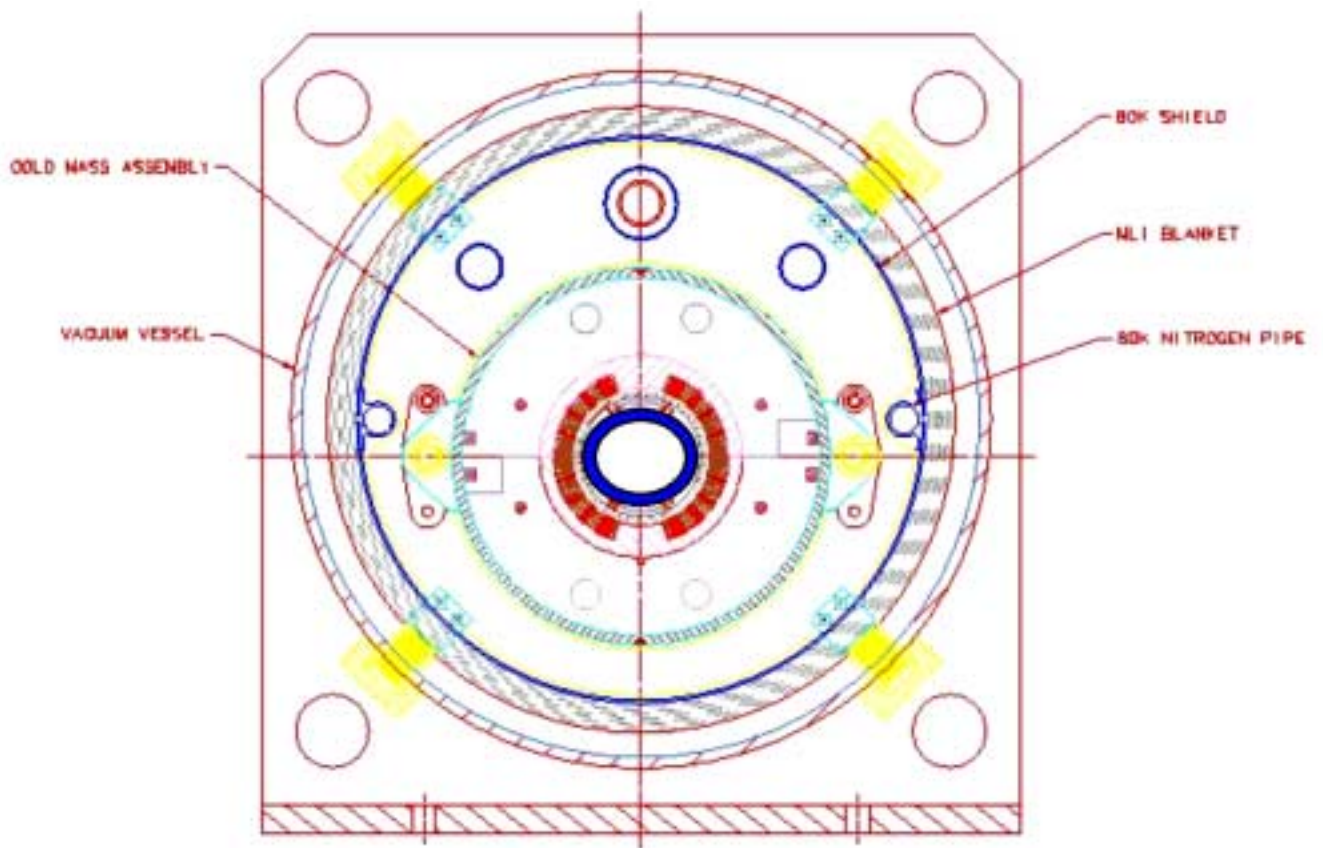
126 m production straight s  
beam angular spread and u



126 m return straight is  
used for injection and other  
machine utility functions.  
Optics details are TBD.

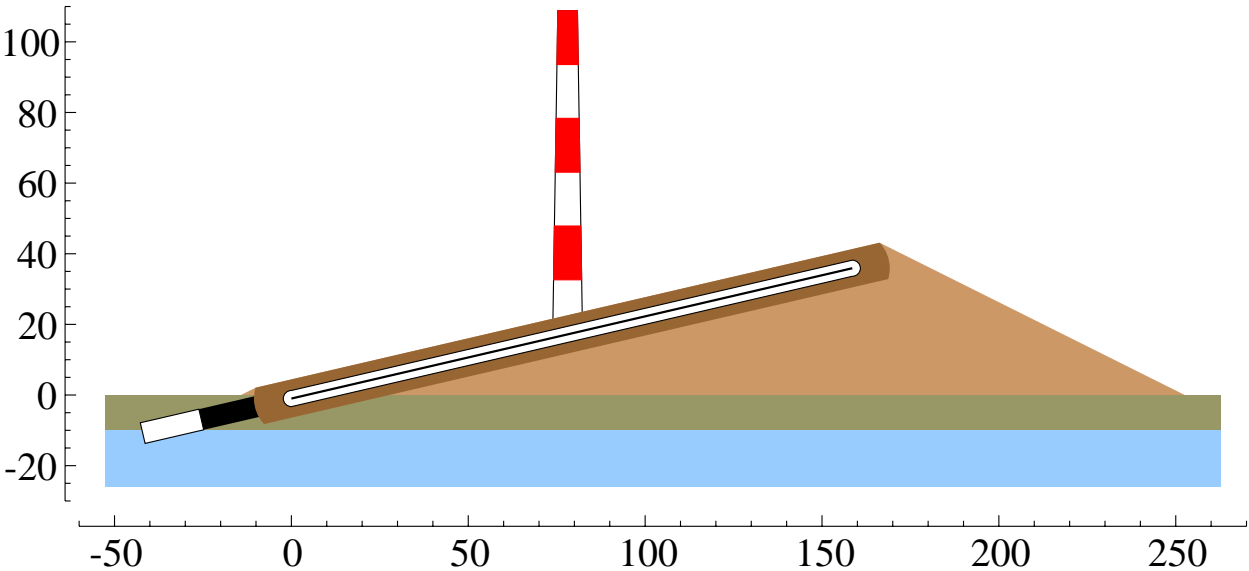
# Alternative Conventional Arcs

- Conventional FODO Lattice
- Cosine Theta Magnets
- Warm W shield inside



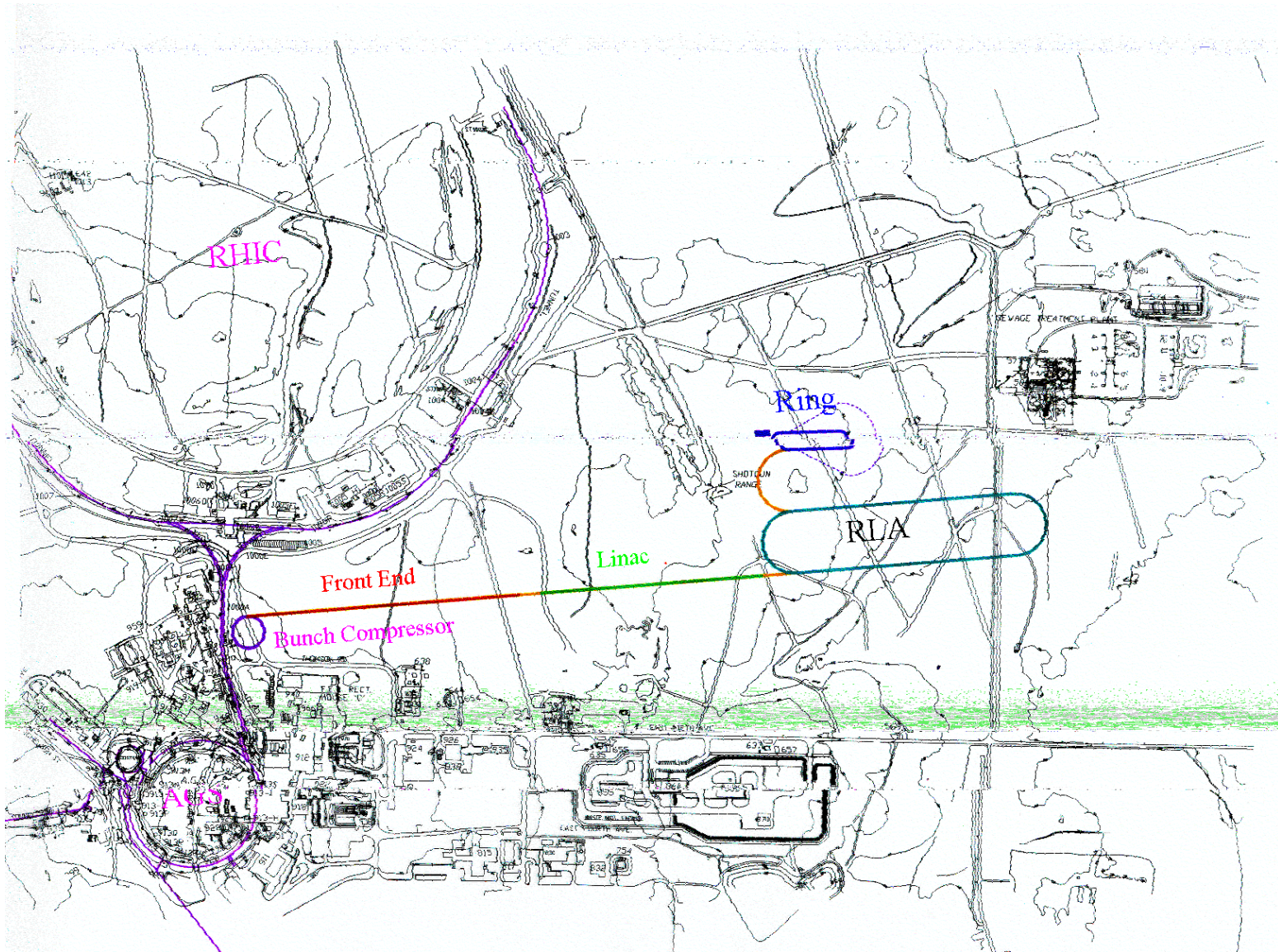
# Ring Layout

To Carlsbad	2903	km
Dip angle	13.1	deg
straight	116	m
circ	332	m
decay/circ	35	%
To Homestake	2528	km
Dip angle	11.4	deg
straight	138	m
circ	376	m
decay/circ	37	%
To Soudan	1713	km
Dip angle	7.73	deg
straight	218	m
circ	536	m
decay/circ	40	%





# BNL Footprint



# FRONT END SIMULATION

Up to and including match to acceleration linac,  
(as remembered by Bob Palmer)

- **Pion Production & radiation**
  - MARS code
  - Checked against 2 other codes
  - Checked against Collaboration AGS Exp E910
  - differences  $\approx 20\%$
- **Target Geometry**
  - Gaussian p beam
  - cylindrical Hg target<sup>1</sup>
  - tilts as specified
- **Tracking through phase rotation and cooling**
  - design code: ICOOL
  - tracking in 3D, including spin
  - decays pi-mu, mu-e
  - statistics to 50,000 in, 10,000 out
  - confirmation by DP GEANT
  - tracking differences  $\leq 5\%$
  - most error studies by DP GEANT

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<sup>1</sup>no distortion or turbulence

- Magnetic Fields

- Field Maps from coil geometries
  - \* capture
  - \* periodic transport
  - \* field flips in phase rotation
  - \* Cooling lattice
  - \* matching between each

- RF Fields

- Analytic pill-box time dependent<sup>2</sup>

- Materials Interactions

- dedx: Bethe Block with density effect
- scatter: Moliere with Rutherford limit<sup>3</sup>
- straggle: Vavilov + gaussian and Landau limits

- Material geometries

- H2 with hemispherical ends<sup>4</sup>
- Al windows with constant thicknesses as specified<sup>5</sup>
- stepped RF Be windows as specified

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<sup>2</sup>noses and rounded outside shape not included, but expected to have negligible effect

<sup>3</sup>some questions remaining on possible overestimate of hard scattering

<sup>4</sup>Study done off line found results insensitive to shape

<sup>5</sup>not tapered



- Errors

- coil currents
- coil transverse positions
- coil tilts
- H2 densities
- no significant effects with engineering tolerances and no steering

- Overall uncertainty  $\approx 30\%$

## FRONT END PERFORMANCE

	p energy GeV	$\mu/p$	$\mu/p/\text{GeV}$ %/GeV
Study 1	16	0.018	.11
Study 2	24	0.17	.71

Total efficiency gain  $\approx 6 \times$

- No change per MW from 24 vs 16 GeV
- From use of the mercury:  $1.9 \times$
- From phase rotation  $\approx 2 \times$
- From cooling design:  $\approx 1.4 \times$
- From larger acceptance:  $1.2 \times$

# IMPROVEMENTS ?

- Longitudinal Cooling(Emittance exchange)
  - Less loss:  $\approx 2 \times \mu/p$
  - Cheaper acceleration ?
  - Progress (Thursday)
- Bunch Beam Phase Rotation
  - both signs
  - Reduced Cost
  - Progress (Thursday)
- FFAG Acceleration
  - larger acceptance ?
  - lower cost ?
  - Progress (Thursday)
- Others

# CONCLUSIONS

- BNL (like FNAL) is a good site for a factory
- Study 2 has  $6 \times$  efficiency of study 1
- Upgrade to 4 MW (factor of 4)
- Efficiency gains probable
- Cost reduction probable
- Big step to a Neutrino Factory
- Small step to a Muon Collider